


Classification

Jarek Szlichta

<http://data.science.uoit.ca/>

Classification: Basic Concepts

- Classification: Basic Concepts 
- Decision Tree Induction
- Bayes Classification Methods
- Rule-Based Classification
- Model Evaluation and Selection
- Techniques to Improve Classification Accuracy:
Ensemble Methods
- Summary

Supervised vs. Unsupervised Learning

- Supervised learning (classification)
 - Supervision: The training data (observations, measurements, etc.) are accompanied by **labels** indicating the class of the observations
 - New data is classified based on the training set
- Unsupervised learning (clustering)
 - The class labels of training data is unknown
 - Given a set of measurements, observations, etc. with the aim of establishing the existence of classes or clusters in the data

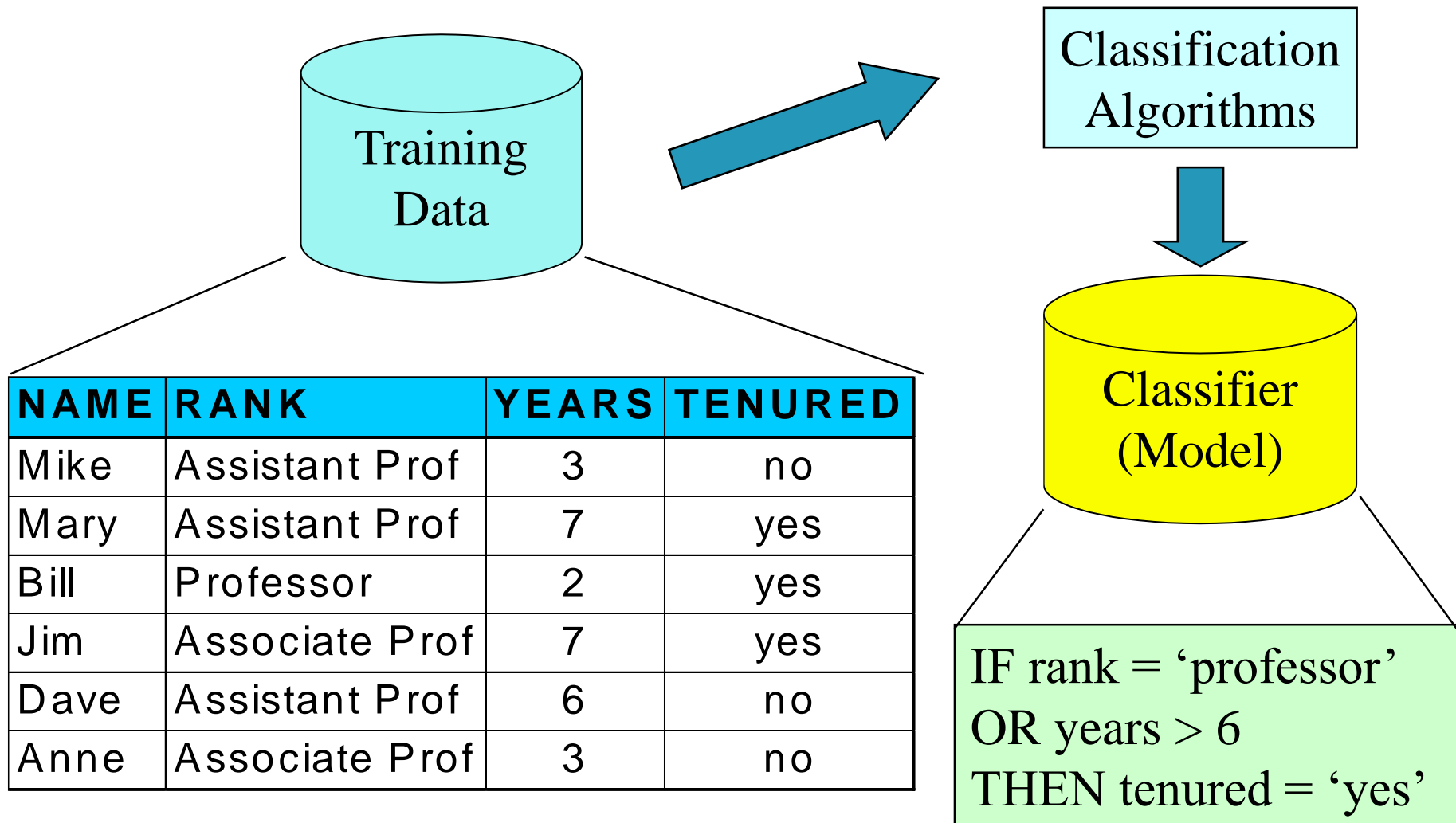
Prediction Problems: Classification vs. Numeric Prediction

- **Classification**
 - predicts categorical class labels (discrete or nominal)
 - classifies data (constructs a model) based on the training set and the values (**class labels**) in a classifying attribute and uses it in classifying new data
- **Numeric Prediction (Regression)**
 - models continuous-valued functions, i.e., predicts unknown or missing values
- **Typical applications**
 - Credit/loan approval:
 - Medical diagnosis: if a tumor is cancerous or benign
 - Fraud detection: if a transaction is fraudulent
 - Web page categorization: which category it is

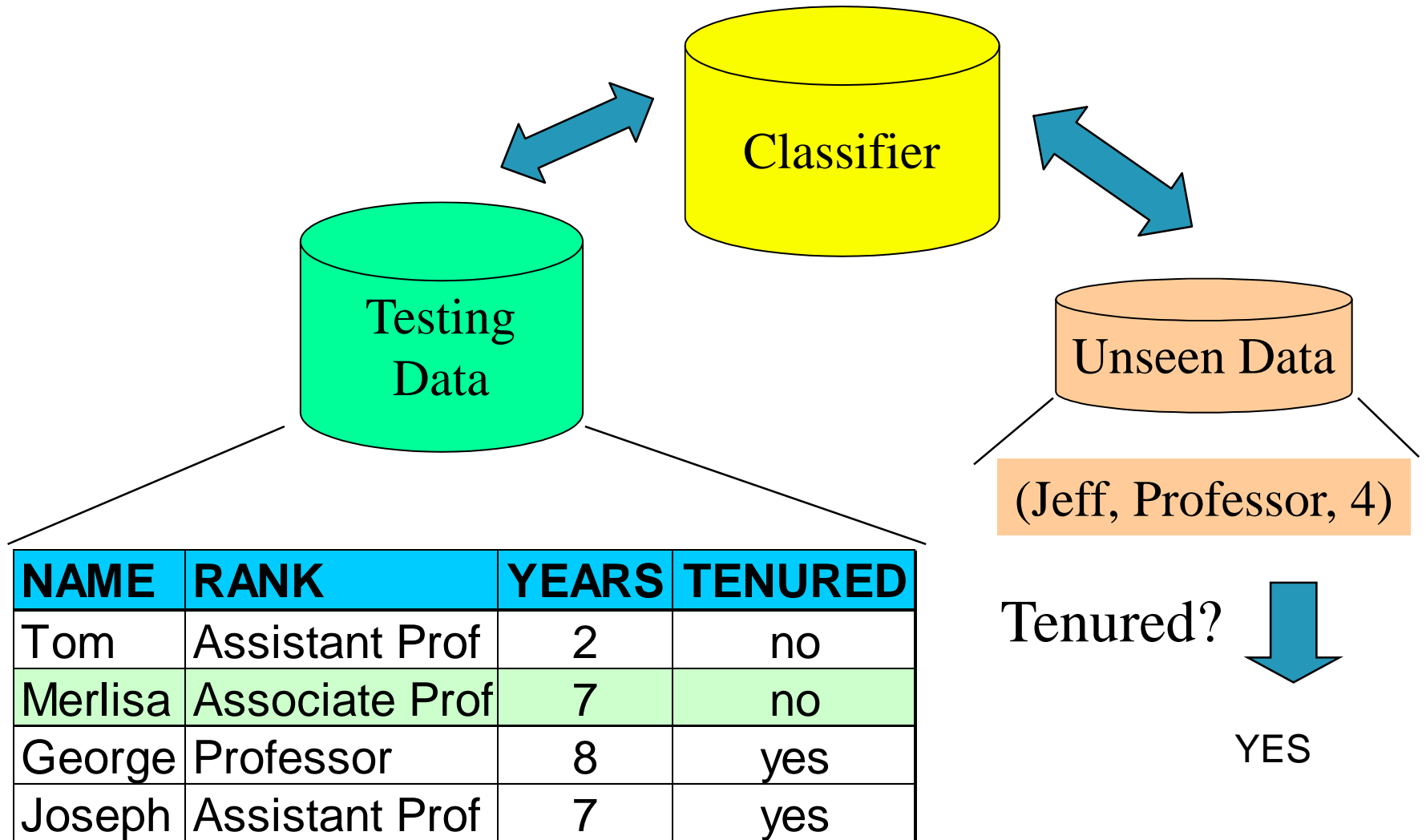
Classification—A Two-Step Process

- **Model construction:** describing a set of predetermined classes
 - Each tuple/sample is assumed to belong to a predefined class, as determined by the **class label attribute**
 - The set of tuples used for model construction is **training set**
 - The model is represented as classification rules, decision trees, or mathematical formula
- **Model usage:** for classifying future or unknown objects
 - **Estimate accuracy** of the model
 - The known label of test sample is compared with the classified result from the model
 - **Accuracy** rate is the percentage of test set samples that are correctly classified by the model
 - **Test set** is independent of training set (otherwise overfitting)
 - If the accuracy is acceptable, use the model to **classify data** tuples whose class labels are not known


Process (1): Model Construction



Process (2): Using the Model in Prediction



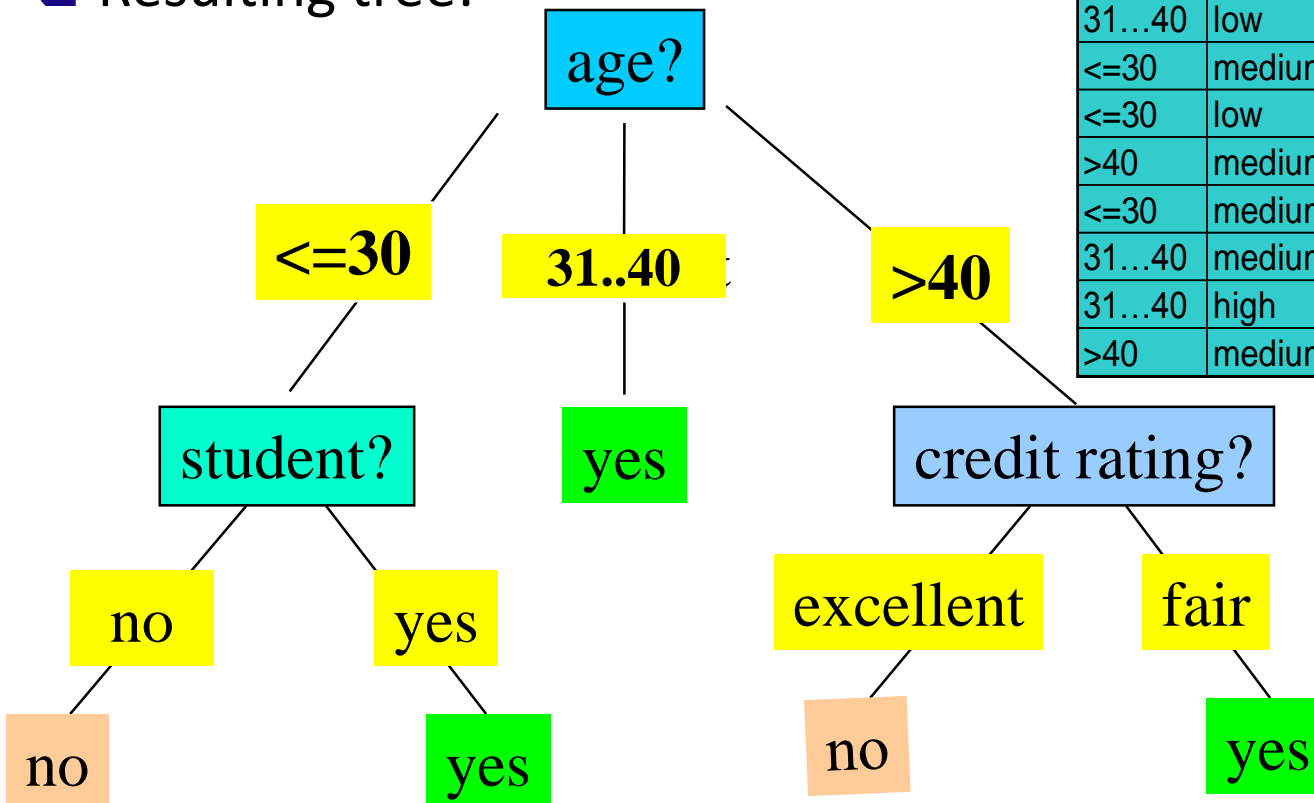
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Decision Tree Induction: An Example

- ❑ Training data set: Buys_computer
- ❑ The data set follows an example of Quinlan's ID3
- ❑ Resulting tree:

| age | income | student | credit_rating | buys_computer |
|---------|--------|---------|---------------|---------------|
| <=30 | high | no | fair | no |
| <=30 | high | no | excellent | no |
| 31...40 | high | no | fair | yes |
| >40 | medium | no | fair | yes |
| >40 | low | yes | fair | yes |
| >40 | low | yes | excellent | no |
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Algorithm for Decision Tree Induction

- Basic algorithm (a greedy algorithm)
 - Tree is constructed in a **top-down recursive divide-and-conquer manner**
 - At start, all the training examples are at the root
 - Attributes are categorical (if continuous-valued, they are discretized in advance)
 - Examples are partitioned recursively based on selected attributes
 - Test attributes are selected on the basis of a heuristic or statistical measure (e.g., **information gain**)
- Conditions for stopping partitioning
 - All samples for a given node belong to the same class
 - There are no remaining attributes for further partitioning – **majority voting** is employed for classifying the leaf
 - There are no samples left

Attribute Selection Measure: Information Gain (ID3/C4.5)

- Select the attribute with the highest information gain
- Let p_i be the probability that an arbitrary tuple in dataset D belongs to class C_i , estimated by $|C_i|/|D|$
- Expected information (entropy) needed to classify a tuple in D:

$$Info(D) = -\sum_{i=1}^m p_i \log_2(p_i)$$

- Information needed (after using attribute A to split dataset D into v partitions) to classify D:
$$Info_A(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times Info(D_j)$$
- Information gained by branching on attribute A

$$Gain(A) = Info(D) - Info_A(D)$$

Attribute Selection: Information Gain

■ Class P: buys_computer = “yes”

■ Class N: buys_computer = “no”

$$Info(D) = I(9,5) = -\frac{9}{14}\log_2\left(\frac{9}{14}\right) - \frac{5}{14}\log_2\left(\frac{5}{14}\right) = 0.940$$

| age | income | student | credit_rating | buys_computer |
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| age | p _i | n _i | I(p _i , n _i) |
|---------|----------------|----------------|-------------------------------------|
| <=30 | 2 | 3 | 0.971 |
| 31...40 | 4 | 0 | 0 |
| >40 | 3 | 2 | 0.971 |

$$\begin{aligned}
 Info_{age}(D) &= \frac{5}{14} \times \left(-\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5}\right) \\
 &\quad + \frac{4}{14} \times \left(-\frac{4}{4} \log_2 \frac{4}{4} - \frac{0}{4} \log_2 \frac{0}{4}\right) \\
 &\quad + \frac{5}{14} \times \left(-\frac{3}{5} \log_2 \frac{3}{5} - \frac{2}{5} \log_2 \frac{2}{5}\right) \\
 &= 0.694 \text{ bits.}
 \end{aligned}$$

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| age | p_i | n_i | $I(p_i, n_i)$ |
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 &= 0.694 \text{ bits.}
 \end{aligned}$$

Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

| age | income | student | credit_rating | buys_computer |
|-----------|--------|---------|---------------|---------------|
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Similarly,

$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit_rating) = 0.048$$

Gain Ratio for Attribute Selection (C4.5)

- Information gain measure is biased towards attributes with a large number of values
- C4.5 (a successor of ID3) uses gain ratio to overcome the problem (normalization to information gain)

$$SplitInfo_A(D) = -\sum_{j=1}^v \frac{|D_j|}{|D|} \times \log_2\left(\frac{|D_j|}{|D|}\right)$$

- $GainRatio(A) = Gain(A)/SplitInfo(A)$
- Ex.
$$SplitInfo_{income}(D) = -\frac{4}{14} \times \log_2\left(\frac{4}{14}\right) - \frac{6}{14} \times \log_2\left(\frac{6}{14}\right) - \frac{4}{14} \times \log_2\left(\frac{4}{14}\right) = 1.557$$
- $gain_ratio(income) = 0.029/1.557 = 0.019$
- The attribute with the maximum gain ratio is selected as the splitting attribute

Comparing Attribute Selection Measures

- The two measures, in general, return good results but
 - **Information gain:**
 - biased towards multivalued attributes
 - **Gain ratio:**
 - tends to prefer unbalanced splits in which one partition is much smaller than the others

Overfitting and Tree Pruning

- Overfitting: An induced tree may overfit the training data
 - Too many branches, some may reflect anomalies due to noise or outliers
 - Poor accuracy for unseen samples
- Two approaches to avoid overfitting
 - Prepruning: *Halt tree construction early*-do not split a node if this would result in the goodness measure falling below a threshold
 - Difficult to choose an appropriate threshold
 - Postpruning: *Remove branches* from a “fully grown” tree—get a sequence of progressively pruned trees
 - Use a set of data different from the training data to decide which is the “best pruned tree”

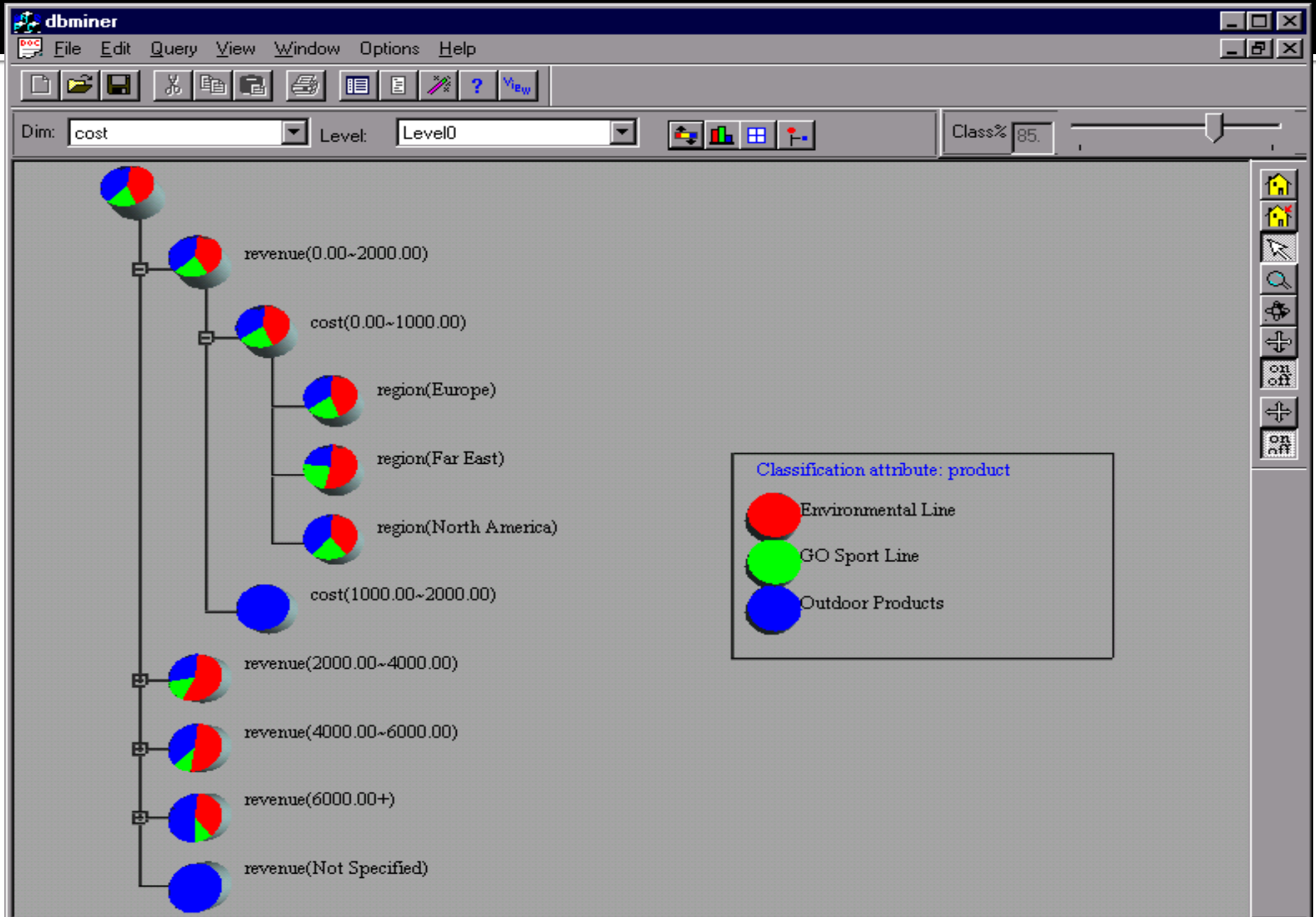
Enhancements to Basic Decision Tree Induction

- Allow for **continuous-valued attributes**
 - Dynamically define new discrete-valued attributes that partition the continuous attribute value into a discrete set of intervals
- Handle **missing attribute values**
 - Assign the most common value of the attribute
- **Attribute construction**
 - Create new attributes based on existing ones that are sparsely represented
 - This reduces fragmentation, repetition, and replication

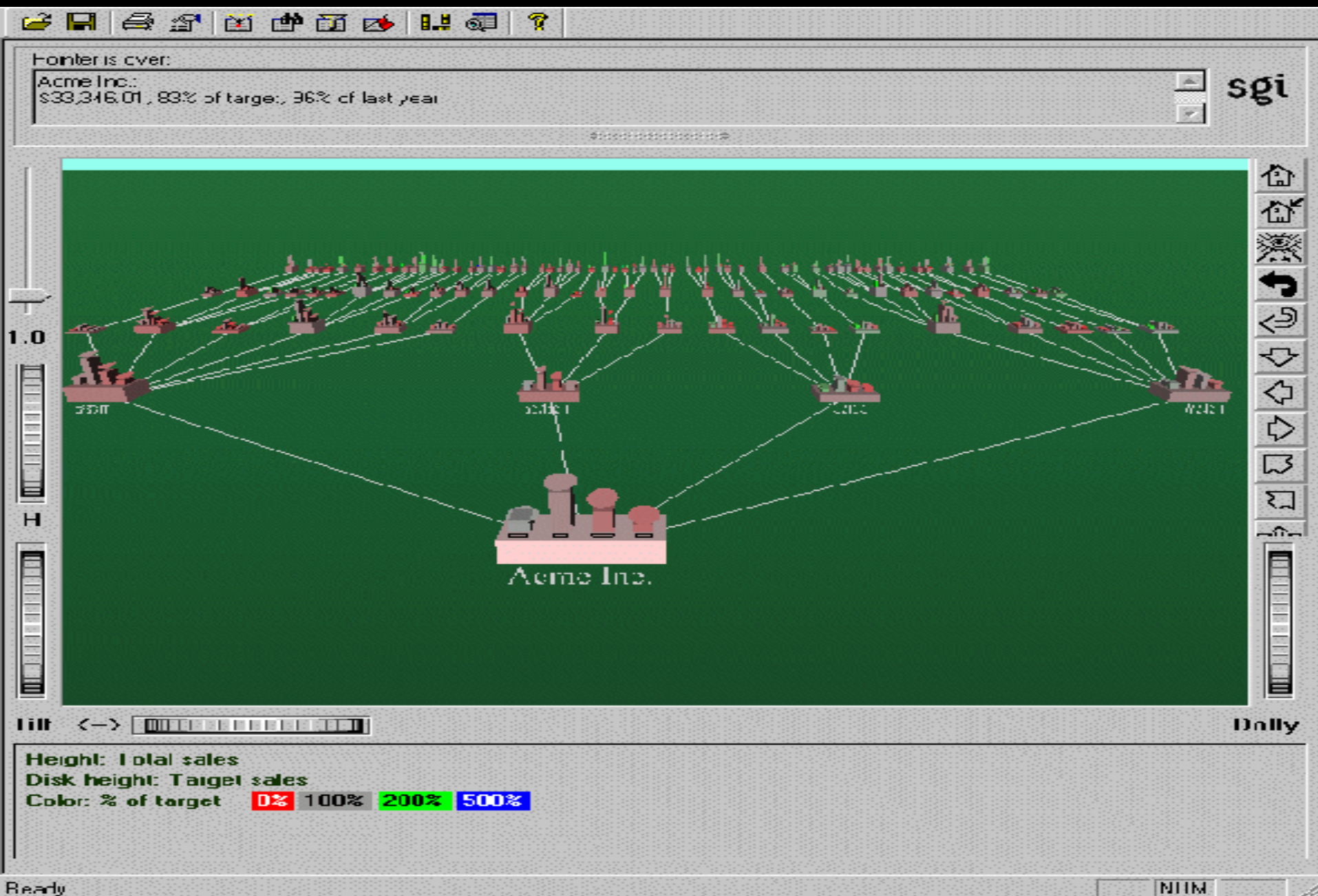
Classification in Large Databases

- Classification—a classical problem extensively studied by statisticians and machine learning researchers
- Scalability: Classifying data sets with millions of examples and hundreds of attributes with reasonable speed
- Why is decision tree induction popular?
 - relatively faster learning speed (than other classification methods)
 - convertible to simple and easy to understand classification rules
 - can use SQL queries for accessing databases
 - comparable classification accuracy with other methods


Presentation of Classification Results



Visualization of a Decision Tree in SGI/MineSet 3.0



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Bayesian Classification: Why?

- A statistical classifier: performs *probabilistic prediction*, i.e., predicts class membership probabilities
- Foundation: Based on Bayes' Theorem.
- Performance: A simple Bayesian classifier, *naïve Bayesian classifier*, has comparable performance with decision tree and Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct — prior knowledge can be combined with observed data
- Standard: Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

Bayesian Theorem: Basics

- Let \mathbf{X} be a data sample (“evidence”): class label is unknown
- Let H be a *hypothesis* that X belongs to class C
- Classification is to determine $P(H|\mathbf{X})$, (*posteriori probability*), the probability that the hypothesis holds given the observed data sample \mathbf{X}
- $P(H)$ (*prior probability*), the initial probability
 - E.g., \mathbf{X} will buy computer, regardless of age, income, ...
- $P(\mathbf{X})$: probability that sample data is observed
- $P(\mathbf{X}|H)$ (likelihood), the probability of observing the sample \mathbf{X} , given that the hypothesis holds
 - E.g., Given that \mathbf{X} will buy computer, the prob. that X is 31..40, medium income

Bayesian Theorem

- Given training data \mathbf{X} , *posteriori probability of a hypothesis* H , $P(H|\mathbf{X})$, follows the Bayes theorem

$$P(H|\mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})} = P(\mathbf{X}|H) \times P(H) / P(\mathbf{X})$$

- Informally, this can be written as

posteriori = likelihood x prior/evidence

- Predicts \mathbf{X} belongs to C_i iff the probability $P(C_i|\mathbf{X})$ is the highest among all the $P(C_k|\mathbf{X})$ for all the k classes
- Practical difficulty: require initial knowledge of many probabilities, significant computational cost

Towards Naïve Bayesian Classifier

- Let D be a training set of tuples and their associated class labels, and each tuple is represented by an n -D attribute vector $\mathbf{X} = (x_1, x_2, \dots, x_n)$
- Suppose there are m classes C_1, C_2, \dots, C_m .
- Classification is to derive the maximum posteriori, i.e., the maximal $P(C_i|\mathbf{X})$
- This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

- Since $P(\mathbf{X})$ is constant for all classes, only

needs to be maximized

$$P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$$

Derivation of Naïve Bayes Classifier

- A simplified assumption: attributes are conditionally independent (i.e., no dependence relation between attributes):
$$P(\mathbf{X} | C_i) = \prod_{k=1}^n P(x_k | C_i) = P(x_1 | C_i) \times P(x_2 | C_i) \times \dots \times P(x_n | C_i)$$
- This greatly reduces the computation cost: Only counts the class distribution

Naïve Bayesian Classifier: Training Dataset

Class:

C1:buys_computer = 'yes'

C2:buys_computer = 'no'

Data sample

X = (age <=30,

Income = medium,

Student = yes

Credit_rating = Fair)

| age | income | student | credit_rating | buys_computer |
|---------|--------|---------|---------------|---------------|
| <=30 | high | no | fair | no |
| <=30 | high | no | excellent | no |
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Naïve Bayesian Classifier: An Example

- $P(C_i)$: $P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$
 $P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$
 - Compute $P(X|C_i)$ for each class
 - $P(\text{age} = \text{"<=30"} \mid \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$
 - $P(\text{age} = \text{"<= 30"} \mid \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$
 - $P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$
 - $P(\text{income} = \text{"medium"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$
 - $P(\text{student} = \text{"yes"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$
 - $P(\text{student} = \text{"yes"} \mid \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$
 - $P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$
 - $P(\text{credit_rating} = \text{"fair"} \mid \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$
 - **$X = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$**
 - $P(X|C_i)$** : $P(X \mid \text{buys_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$
 $P(X \mid \text{buys_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$
 - $P(X|C_i) \cdot P(C_i)$** : $P(X \mid \text{buys_computer} = \text{"yes"}) \cdot P(\text{buys_computer} = \text{"yes"}) = 0.028$
 $P(X \mid \text{buys_computer} = \text{"no"}) \cdot P(\text{buys_computer} = \text{"no"}) = 0.007$
- Therefore, X belongs to class ("buys_computer = yes")**

Avoiding the Zero-Probability Problem

- Naïve Bayesian prediction requires each conditional prob. be **non-zero**. Otherwise, the predicted prob. will be zero

$$P(X | C_i) = \prod_{k=1}^n P(x_k | C_i)$$

- Ex. Suppose a dataset with 1000 tuples, income=low (0), income= medium (990), and income = high (10)
- Use **Laplacian correction** (or Laplacian estimator)

- *Adding 1 to each case*

Prob(income = low) = 1/1003

Prob(income = medium) = 991/1003


Prob(income = high) = 11/1003

- The “corrected” prob. estimates are close to their “uncorrected” counterparts

Naïve Bayesian Classifier: Comments

- Advantages
 - Easy to implement
 - Good results obtained in most of the cases
- Disadvantages
 - Assumption: class conditional independence, therefore loss of accuracy
 - Practically, dependencies exist among variables
 - E.g., Symptoms: fever, cough etc., Disease: lung cancer, diabetes, etc.
 - Dependencies among these cannot be modeled by Naïve Bayesian Classifier
- How to deal with these dependencies? Bayesian Belief Networks (Chapter 9 in the text book)

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Using IF-THEN Rules for Classification

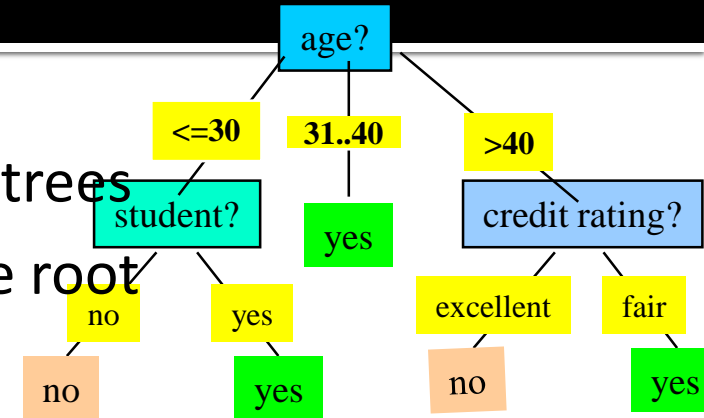
- Represent the knowledge in the form of IF-THEN rules

R: IF *age* = youth AND *student* = yes THEN *buys_computer* = yes

 - Rule antecedent/precondition vs. rule consequent
- Assessment of a rule: *coverage* and *accuracy*
 - n_{covers} = # of tuples covered by R
 - n_{correct} = # of tuples correctly classified by R
- If more than one rule are triggered, need **conflict resolution**
 - Size ordering: assign the highest priority to the triggering rules that has the “toughest” requirement (i.e., with the *most attribute tests*)
 - Rule-based ordering (**decision list**): rules are organized into one long priority list, according to some measure of rule quality or by experts

Rule Extraction from a Decision Tree

- Rules are *easier to understand* than large trees
- One rule is created *for each path* from the root to a leaf
- Each attribute-value pair along a path forms a conjunction: the leaf holds the class prediction
- Rules are mutually exclusive and exhaustive
- Example: Rule extraction from our *buys_computer* decision-tree



IF *age* = young AND *student* = *no*

THEN *buys_computer* = *no*

IF *age* = young AND *student* = *yes*

THEN *buys_computer* = *yes*

IF *age* = mid-age

THEN *buys_computer* = *yes*


IF *age* = old AND *credit_rating* = *excellent*

THEN *buys_computer* = *no*

IF *age* = old AND *credit_rating* = *fair*

THEN *buys_computer* = *yes*

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Model Evaluation and Selection

- Evaluation metrics: How can we measure accuracy? Other metrics to consider?
- Use **test set** of class-labeled tuples instead of training set when assessing accuracy
- Methods for estimating a classifier's accuracy:
 - Holdout method, random subsampling
 - Cross-validation

Classifier Evaluation Metrics: Confusion Matrix

Confusion Matrix:

| Actual class\Predicted class | C_1 | $\neg C_1$ |
|------------------------------|----------------------|----------------------|
| C_1 | True Positives (TP) | False Negatives (FN) |
| $\neg C_1$ | False Positives (FP) | True Negatives (TN) |

Example of Confusion Matrix:

| Actual class\Predicted class | buy_computer = yes | buy_computer = no | Total |
|------------------------------|--------------------|-------------------|-------|
| buy_computer = yes | 6954 | 46 | 7000 |
| buy_computer = no | 412 | 2588 | 3000 |
| Total | 7366 | 2634 | 10000 |

- Given m classes, an entry, $CM_{i,j}$ in a **confusion matrix** indicates # of tuples in class i that were labeled by the classifier as class j
- May have extra rows/columns to provide totals

Accuracy, Error Rate, Sensitivity and Specificity

| A\P | C | ¬C | |
|-----|----|----|-----|
| C | TP | FN | P |
| ¬C | FP | TN | N |
| | P' | N' | All |

- **Classifier Accuracy**, or recognition rate: percentage of test set tuples that are correctly classified

$$\text{Accuracy} = (TP + TN)/All$$

- **Error rate**: $1 - \text{accuracy}$, or
$$\text{Error rate} = (FP + FN)/All$$

- **Class Imbalance Problem:**

- One class may be *rare*, e.g. fraud, or HIV-positive
- Significant *majority of the negative class* and minority of the positive class
- **Sensitivity**: True Positive recognition rate
 - **Sensitivity** = TP/P
- **Specificity**: True Negative recognition rate
 - **Specificity** = TN/N

Precision and Recall, and F-measures

- **Precision:** exactness – what % of tuples that the classifier labeled as positive are actually positive

$$precision = \frac{TP}{TP + FP}$$

- **Recall:** completeness – what % of positive tuples did the classifier label as positive?

$$recall = \frac{TP}{TP + FN}$$

- Perfect score is 1.0

- **F measure (F_1 or F-score):** harmonic mean of precision and recall,

$$F = \frac{2 \times precision \times recall}{precision + recall}$$

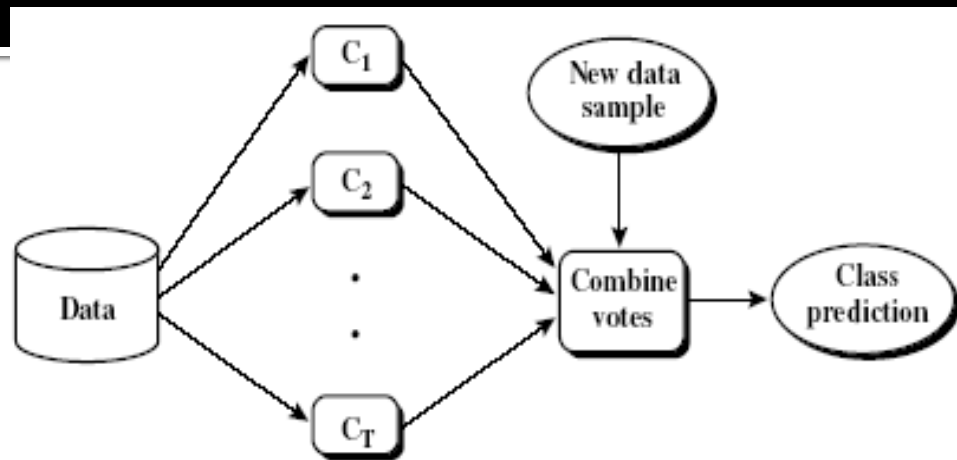
Classifier Evaluation Metrics: Example

| Actual Class\Predicted class | cancer = yes | cancer = no | Total | Recognition(%) |
|------------------------------|--------------|-------------|-------|------------------------------|
| cancer = yes | 90 | 210 | 300 | 30.00 (<i>sensitivity</i>) |
| cancer = no | 140 | 9560 | 9700 | 98.56 (<i>specificity</i>) |
| Total | 230 | 9770 | 10000 | 96.40 (<i>accuracy</i>) |

- $Precision = 90/230 = 39.13\%$

$$Recall = 90/300 = 30.00\%$$

Ensemble Methods: Increasing the Accuracy



- Ensemble methods
 - Use a combination of models to increase accuracy
 - Combine a series of k learned models, M_1, M_2, \dots, M_k , with the aim of creating an improved model M^*
- Popular ensemble methods
 - Bagging: averaging the prediction over a collection of classifiers
 - Boosting: weighted vote with a collection of classifiers

Summary (I)

- **Classification** is a form of data analysis that extracts **models** describing important data classes.
- Effective and scalable methods have been developed for **decision tree induction**, **Naive Bayesian classification**, **rule-based classification**, and many other classification methods.
- **Evaluation metrics** include: accuracy, sensitivity, specificity, precision, recall, F measure.
- **Stratified k-fold cross-validation** is recommended for accuracy estimation. **Bagging** and **boosting** can be used to increase overall accuracy by learning and combining a series of individual models.

Summary (II)

- No single method has been found to be superior over all others for all data sets
- Issues such as accuracy, training time, robustness, scalability, and interpretability must be considered and can involve trade-offs, further complicating the quest for an overall superior method

Reading List

- Recommended

- Review Slides!
- Book: Jiawei Han, Micheline Kamber and Jian Pei, Data Mining - Concepts and Techniques, Morgan Kaufmann, Third Edition, 2011 (or 2nd edition)
 - http://ccs1.hnue.edu.vn/hungtd/DM2012/DataMining_BOOK.pdf
 - Chapter: 8